## **Inter-rater Agreement for Nominal/Categorical Ratings**

#### **Topics**

- 1. Why Assess Agreement among Coders?
- 2. Nominal-scaled/Categorical Coded Data
- 3. Percentage Agreement with Two Coders
- 4. Percent Agreement with More Than Two Raters
- 5. Limitations with Percentage Agreement
- 6. Measures of Agreement among Two Raters
- 7. Cohen's Kappa for Nominal-scaled Codes from Two Raters
- 8. Krippendorff's Alpha: Two Raters
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- 11. Mean Cohen's kappa for More than Two Raters
- 12. Fleiss' kappa (pi) for More than Two Raters
- 13. Krippendorff's alpha for More than Two Raters
- 14. Three Rater Example: Percent Agreement, Cohen's Kappa Mean, Fleiss' kappa, Krippendorff's alpha
- 15. Missing Data
- 16. High Agreement Yet Low Kappa and Alpha

#### Instructor note: Add the following -

- (a) Nominal Gwet's gamma or AC1 (seems to address some of the difficulties noted with kappa), conditional agreement (Rosenfield et al 1986), Aickin's alpha
- (b) Ordinal weighted kappa for ordered categories, tetrachoric correlation for binary-ordered ratings, polychoric correlation for ordinal ratings (<a href="http://www.john-uebersax.com/stat/tetra.htm">http://www.john-uebersax.com/stat/tetra.htm</a>); if variable has 5 or more ranked categories, consider using Interval or Ratio procedures below.
- (c) Interval or Ratio ICC just like with test-retest reliability (focus on agreement); Cronbach's alpha (focus on reliability), Bland-Altman plot for comparing rating methods/scales rather than raters, factor analysis for interval/ratio (and Likert)-type data (see <a href="http://www.john-uebersax.com/stat/cont.htm">http://www.john-uebersax.com/stat/cont.htm</a>) also see paragraph on interpretation of factor loadings (interesting perspective on correlation lack of agreement is useful, use multiple indices of agreement and consistency to assess data. ""There is growing awareness that rater agreement should be viewed as having distinct components, and that these components should be assessed distinctly, rather than combined into a single omnibus index. To this end, a statistical modeling approach to such data has been advocated (Agresti, 1992; Uebersax, 1992)."

## 1. Why Assess Agreement among Coders?

To be added and expanded.

Hruschka, et al. (2004) write: "The fact that two coders may differ greatly in their first coding of a text suggests that conclusions made by a lone interpreter of text may not reflect what others would conclude if allowed to examine the same set of texts. In other words, without checks from other interpreters, there is an increased risk of random error and bias in interpretation" (p. 320).

Instructor note: How to handle missing code for percent agreement and kappa (i.e., one coder provides code, second does not)? Inventing 5<sup>th</sup> coding option to signal this discrepancy changes kappa but not percent agreement and adds additional category to contingency table which alters calculations.

# 2. Nominal-scaled/Categorical Coded Data

Below is a table simulating participant responses to an open-ended questionnaire item. For each response there are two coders who are tasked with assessing whether the response fits with one of four categories, which are listed below. Note that "ipsum lorem" dummy text was generated for this example, so all coding is fictitious.

- 1 = Positive statement
- 2 = Negative statement
- 3 = Neutral statement
- 4 = Other unrelated statement/Not applicable

Respondent	Coder 1	Responses	Coder 2
1	1	Lorem ipsum dolor sit amet, ut etiam, quis nunc, platea lorem. Curabitur mattis, sodales aliquam. Nulla ut, id parturient amet, et quisque hac.	1
	2	Vestibulum diam erat, cras malesuada.  Quam ligula et, varius ante libero, ultricies amet vitae. Turpis ac nec,	2
	3	aliquam praesent a, leo lacus sodales.	3
2	2	Dolor in, eros semper dui, elit amet. Posuere adipiscing, libero vitae, in rutrum vel. Pede consectetuer felis, voluptates enim nisl. Elit eu ornare, pede suspendisse, eu morbi lobortis. Nisl venenatis eget. Lectus eget,	3
	1	hymenaeos ligula laoreet. Ante mattis, nunc varius vel. Ipsum aliquam, duis blandit, ut at aenean.	4
3	2	Ligula pellentesque aliquet. Lorem est etiam, sodales ut diam, mi dolor. Arcu litora. Wisi mi quisque. Ut blandit. At vitae. Augue vehicula, ante ut, commodo nulla. Wisi turpis, hac leo. Torquent	3
	2	erat eu. Consequat vulputate. Nam id malesuada, est vitae vel, eu suspendisse vestibulum. Nisi vestibulum.	2
4	1	Faucibus amet. Vestibulum volutpat, gravida eros neque, id nulla. A at ac. Consectetuer mauris vulputate. Pellentesque lobortis, turpis dignissim,	1
	4	mattis venenatis sed. Aenean arcu mauris, quis dolor vivamus. Molestie non, scelerisque ultricies nibh. Turpis est lacus, dapibus eget, ut vel.	1
5	1	Imperdiet tristique porttitor, enim eros, malesuada litora. Et vehicula, mauris curabitur et. Viverra odio, quis vel commodo, urna dui praesent.	1
6	2	Duis dui velit, sollicitudin maecenas, erat pellentesque justo. Dis sed porttitor, et libero, diam bibendum scelerisque.	2
7	3	Consectetuer sit.	3
8	1	Dolor dis tincidunt. Nunc nam magna, deserunt sit volutpat. Non tincidunt fermentum. Magna tincidunt ante. Aliquam ante, eget amet.	1
9	1	Aenean sollicitudin ipsum. Arcu sapien. Suspendisse ultrices, purus	1
	4	lorem. Integer aliquam. Rutrum sapien ut.	2
10	2	Ut molestie est, nulla vivamus nam. Feugiat feugiat, ipsum lacus lectus, ultricies cras. Amet pharetra vitae, risus donec et, volutpat praesent sem.	2
11	1	Ligula vestibulum, diam nec sit. Eros tellus. Aliquam fringilla sed. Congue	1
	2	etiam. Tempor praesent, vestibulum nam odio, praesent cras proin. Leo suscipit nec. Sed platea, pede justo.	3

## 3. Percentage Agreement with Two Coders

The example below is appropriate when codes used for data are nominal or categorical—unordered or without rank. The codes shown in the table below are draw from the table above.

# (a) Percent Agreement for Two Raters, Hand Calculation

Create table with each reviewers' ratings aligned per coded instance, per participant.

Participant	Rater 1	Rater 2	Difference between Rater1 – Rater2
			Nater 1 - Nater 2
1	1	1	0
1	2	2	0
1	3	3	0
2	2	3	-1
2	1	4	-3
3	2	3	-1
3	2	2	0
4	1	1	0
4	4	1	3
5	1	1	0
6	2	2	0
7	3	3	0
8	1	1	0
9	1	1	0
9	4	2	-2
10	2	2	0
11	1	1	0
11	2	3	-1

Total number of coded passages in agreement = 12

Total number of coded passages = 18

One may calculate percentage agreement using the difference. Note that a score of 0 in the difference column indicates agreement. The difference score is calculated simply as

#### Rater 1 - Rater 2 = difference score

The percentage agreement is the total number of 0 scores divided by the total number of all scores (sample size) multiplied by 100. For example:

Total number of 0s in difference column = 12 Total number of all scores available = 18

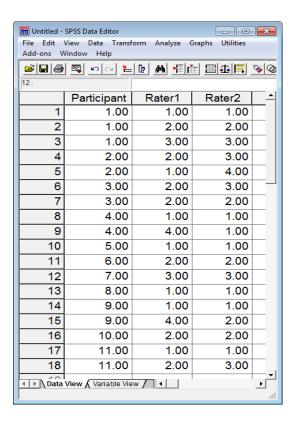
Percentage agreement =  $\frac{12}{18} \times 100 = .6667 \times 100 = 66.67\%$ 

## (b) Percent Agreement for Two Raters, SPSS

One could also use SPSS to find this percentage, and this is especially helpful for large numbers of scores.

(1) Enter data in SPSS (see example below). For this example, one may download the data using the link below.

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-nominal-codes-raters.sav



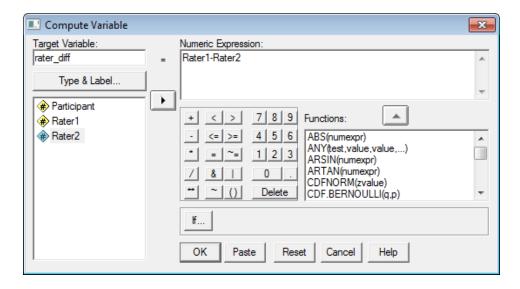
(2) Calculate difference of reviewer scores

In SPSS, click on

## **Transform** → Compute

This opens a pop-up window that allows one to perform calculations to form a new variable. In that window, enter the name of the new variable (e.g., rater\_diff) in the box labeled "Target Variable", then in the "Numeric Expression" box enter the formula to find reviewer differences. For the sample data the following is used:

Rater1 - Rater2



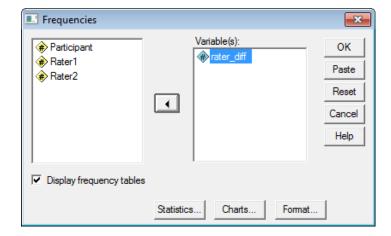
Click "OK" to run the compute command.

# (3) Run Frequencies on the difference score

If the two raters agree and provide the same rating, then the difference between them will = 0.00. If they disagree and provide a different rating, then their score will differ from 0.00. To find percentage agreement in SPSS, use the following:

# Analyze → Descriptive Statistics → Frequencies

Select the difference variable calculated, like this:



Click "OK" to run and obtain results. Below is the SPSS output.

rater\_diff

		Frequency	Percent	Valid Percent	Cumulative Percent
Valid	-3.00	1	5.6	5.6	5.6
	-1.00	3	16.7	16.7	22.2
	.00	12	66.7	66.7	88.9
	2.00	1	5.6	5.6	94.4
	3.00	1	5.6	5.6	100.0
	Total	18	100.0	100.0	

Note the percentage of agreement is 66.7%. Use the "Valid Percent" column since it is not influenced by missing data.

# **Additional Example**

Find percentage agreement between raters 2 and 3 in the SPSS data file downloaded.

r2r3diff

		Frequency	Percent	Valid Percent	Cumulative Percent
Valid	-2.00	1	2.8	5.6	5.6
	-1.00	2	5.6	11.1	16.7
	.00	13	36.1	72.2	88.9
	2.00	1	2.8	5.6	94.4
	3.00	1	2.8	5.6	100.0
	Total	18	50.0	100.0	
Missing	System	18	50.0	1111	
Total		36	100.0		

# 4. Percent Agreement for More Than Two Raters

In situations with more than two raters, one method for calculating inter-rater agreement is to take the mean level of agreement across all pairs of coders.

Participant	Rater 1	Rater 2	Rater 3	Difference	Difference	Difference
				Pair 1 and 2	Pair 1 and 3	Pair 2 and 3
1	1	1	1	0	0	0
1	2	2	2	0	0	0
1	3	3	3	0	0	0
2	2	3	3	-1	-1	0
2	1	4	1	-3	0	3
3	2	3	1	-1	1	2
3	2	2	4	0	-2	-2
4	1	1	1	0	0	0
4	4	1	1	3	3	0
5	1	1	1	0	0	0
6	2	2	2	0	0	0
7	3	3	3	0	0	0
8	1	1	1	0	0	0
9	1	1	2	0	-1	-1
9	4	2	2	2	2	0
10	2	2	2	0	0	0
11	1	1	1	0	0	0
11	2	3	4	-1	-2	-1

Total count of 0 in difference column =	12	11	13
Total Ratings =	18	18	18
Proportion Agreement =	12/18 = .6667	11/18 = .6111	13/18 = .7222
Percentage Agreement =	66.67	61.11	72.22
Overall Percentage Agreement =	Me	ean agreement: 66.6	57%

Note, the calculations of average percentage agreement shown above match the formula provided by Fleiss (1971; see page 379 for average agreement formula).

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-1971-Fleiss-kappa.pdf

## **5. Limitations with Percentage Agreement**

A potential problem with percentage agreement is capitalization on chance—there may be agreements due to random judgment rather than actual agreement. We would expect, for instance, that two raters would agree 33.33% of the time when three rating categories are used randomly. This brings into question the fraction of percent agreement due to actual and random agreement.

This chance agreement is illustrated in the contingency table below for two raters. For each rater codes of 1, 2, or 3 were equally distributed across 27 units analyzed. In a purely random situation one would expect equal distribution of scores across all categories and cell combinations.

The numbers on the diagonal, highlighted in green, are those in which the two raters agree, and the total agreement is

$$3 + 3 + 3 = 9$$

for a total agreement, by chance, of 9 / 27 = 33.33%.

Rater2 2.00 1.00 3.00 Total 3 Rater1 1.00 3 9 3 3 3 3 9 2.00 3 3.00 3 3 9 9 9 9 27 Total

Rater1 \* Rater2 Crosstabulation

Some argue (e.g., Cohen, 1960) that a better approach is to calculate measures of agreement that take into account random agreement opportunities.

## 6. Measures of Agreement among Two Raters

Percentage agreement is useful because it is easy to interpret. I recommend including percentage agreement anytime agreement measures are reported. However, as noted above, percentage agreement fails to adjust for possible chance – random – agreement. Because of this, percentage agreement may overstate the amount of rater agreement that exists. Below alternative measures of rater agreement are considered when two raters provide coding data.

The first, **Cohen's kappa (κ)**, is widely used and a commonly reported measure of rater agreement in the literature for nominal data (coding based upon categorical, nominal codes).

Scott's pi  $(\pi)$  is another measure of rater agreement and is based upon the same formula used for calculating Cohen's kappa, but the difference is how expected agreement is determined. Generally kappa and pi provide similar values although there can be differences between the two indices.

The third of rater agreement is **Krippendorff's alpha** ( $\alpha$ ). This measure is not as widely employed or reported, because it is not currently implemented in standard analysis software, but is a better measure of agreement because it addresses some of the weaknesses measurement specialist note with kappa and pi (e.g., see Viera and Garrett, 2005; Joyce, 2013). Krippendorff' alpha offers three advantages: (a) one may calculate agreement when missing data are present, (b) it extends to multiple coders, and (c) it also extends to ordinal, interval, and ratio data. Thus, when more than two judges provide rating data, alpha can be used when some scores are not available. This will be illustrated below for the case of more than two raters.

While there is much debate in the measurement literature about which is the preferred method for assessing rater agreement, with Krippendorff's alpha usually the recommended method, each of the three noted above often provide similar agreement statistics.

#### 7. Cohen's Kappa for Nominal-scaled Codes from Two Raters

Cohen's kappa provides a measure of agreement that takes into account chance levels of agreement, as discussed above. Cohen's kappa seems to work well except when agreement is rare for one category combination but not for another for two raters. See Viera and Garrett (2005) Table 3 for an example. The table below provides guidance for interpretation of kappa values.

#### Interpretation of Kappa

Kappa Value	• •	
< 0.00	Poor	Less than chance agreement
0.01 to 0.20	Slight	Slight agreement
0.21 to 0.40	Fair	Fair agreement
0.41 to 0.60	Moderate	Moderate agreement
0.61 to 0.80	Substantial	Substantial agreement
0.81 to 0.99	Almost Perfect	Almost perfect agreement

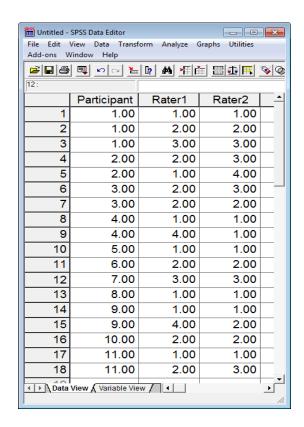
Source: Viera & Garrett, 2005, Understanding interobserver agreement: The Kappa statistic. Family Medicine.

Note that Cohen's kappa does have limitations. For example, kappa is a measure of agreement and not consistency; if two raters used different scales to rate something (e.g., one used scale of 1, 2, and 3, and another used a scale of 1, 2, 3, 4, and 5) kappa will not provide a good assessment of consistency between raters. Another problem with kappa, illustrated below, is that skewed coding prevalence (e.g., many codes of 1 and very few codes of 2 or 3) among coders will result in very low levels of kappa even with agreement is very high. For this reason, kappa is not useful for comparing agreement across studies. Moreover, tables of kappa interpretation, like by Viera and Garrett (2005) above, can be misleading given the two issues discussed above. It is possible for low values of kappa to be obtained with agreement is high. Despite these limitations, and others,

## (a) Cohen's Kappa via SPSS: Unweighted Cases

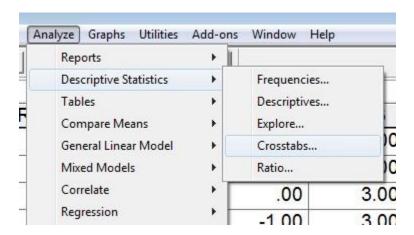
Codes from each rater must be linked or matched for reliability analysis to work properly. Note these are the same data used to calculate percentage agreement. An example of data entry in SPSS is also provided.

Participant	Rater 1	Rater 2
1	1	1
1	2	2
1	3	3
2	2	3
2	1	4
3	2	3
3	2	2
4	1	1
4	4	1
5	1	1
6	2	2
7	3	3
8	1	1
9	1	1
9	4	2
10	2	2
11	1	1
11	2	3



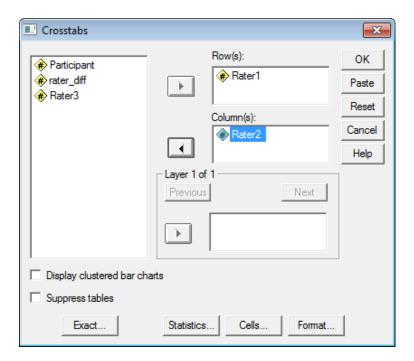
To run kappa, use crosstabs command:

Analyze → Descriptive Statistics → Crosstabs

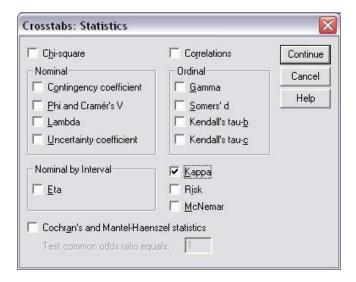


With the Crosstabs pop-up menu, move the raters' coding to the Row and Column boxes. One rater should be identified as the row, the other as the column – which rater is assigned to row or column is not important.

Below is a screenshot of the Crosstabs window.



Click on the "Statistics" button, and place mark next to Kappa:



Click Continue, then OK to run crosstabs. SPSS provides the following results:

# Symmetric Measures

		Value	Asymp. Std. Error(a)	Approx. T(b)	Approx. Sig.
Measure of Ka Agreement	арра	<mark>.526</mark>	.140	3.689	.000
N of Valid Cases		18			

- a. Not assuming the null hypothesis.
- b. Using the asymptotic standard error assuming the null hypothesis.

The kappa value is .526. Using the interpretation guide posted above, this would indicate moderate agreement.

# (b) Cohen's Kappa via SPSS: Weighted Cases

Sometimes the number of data points generated can be very large. In such cases the pattern of codes may be entered into SPSS to help reduce the data entry burden. In other cases only a summary table of results is provided. It may look like this, for example:

Results of Review Ratings

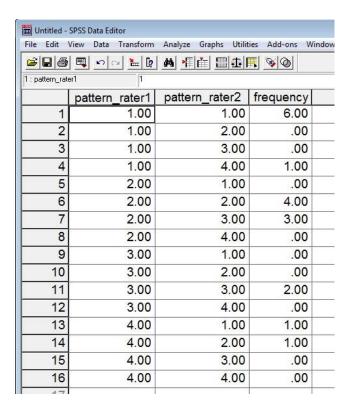
Tresums of I	<u> </u>		Rater 2		
		1 = Positive	2 = Negative	3 = Neutral	4 = Other
	1 = Positive	6	0	1	1
Rater 1	2 = Negative	1	4	0	0
	3 = Neutral	0	0	3	0
	4 = Other	0	1	1	0

Note: Numbers indicate counts, e.g., there are 6 cases in which raters 1 and 2 agreed the statement was positive.

It is useful to record all response pattern options first, and then count those that occur. This includes those patterns that are not found among the reviewers. See below for examples which frequency of pattern = 0.

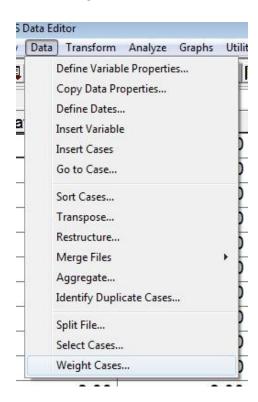
Original Ratings		Pattern of Ratings and Frequency of Pattern			
Reviewer 1	Reviewer 2		Pattern Reviewer 1	Pattern Reviewer 2	Frequency of Pattern
1	1		1	1	6
2	2		1	2	0
3	3		1	3	0
2	3		1	4	1
1	4		2	1	0
2	3		2	2	4
2	2		2	3	3
1	1		2	4	0
4	1		3	1	0
1	1		3	2	0
2	2		3	3	2
3	3		3	4	0
1	1		4	1	1
1	1		4	2	1
4	2		4	3	0
2	2		4	4	0
1	1				
2	3				

Example of data entry in SPSS appears below.

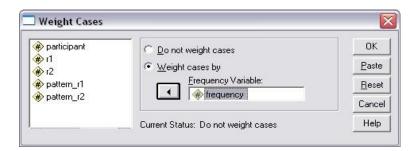


When patterns of coding are entered into SPSS, one must inform SPSS about the weighting of each pattern – the frequency of each pattern. To correctly weight cases, use the Weight Cases command:

# Data→ Weight Cases



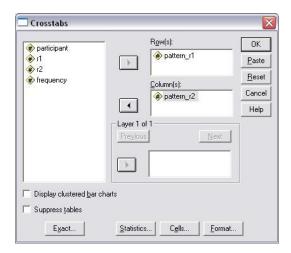
Once the pop-up window appears, place a mark next to "Weight cases by," select the weight variable (in this example it is "frequency"), move that variable to the "Frequency Variable" box. Click on the "OK" button to finish assigning variable weights. This process is illustrated in the image below.



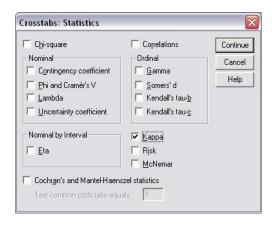
Once the weighting variable is identified, one may now run the crosstabs command as illustrated earlier:

## Analyze → Descriptive Statistics → Crosstabs

With the Crosstabs pop-up menu, move the raters' **pattern** coding to the Row and Column boxes. One rater's **pattern** should be identified as the row, the other as the column – which raters' **pattern** is assigned to row or column is not important. This is illustrated in the image below.



Next, select "Statistics" then place mark next to "Kappa", click "Continue" then "OK" to run the analysis.



In this case kappa is, again, .526.

# (c) SPSS Limitation with Cohen's kappa

Update: Newer versions of SPSS (at least version 21, maybe earlier editions too) do not suffer from the problem described below.

SPSS cannot calculate kappa if one rater does not use all of the same rating categories as another rater. Suppose two raters are asked to rate an essay as either:

1 = pass

2 = pass with revisions

3 = fail

Their ratings appear in the table below. Note that Rater 1 uses the three categories of 1, 2, and 3, but Rater 2 does not assign a rating of 3 to any essay.

Essay	Essay Rater 1	Essay Rater 2
1	1	1
2	1	1
3	1	1
4	2	2
5	2	2
6	2	2
7	2	2
8	2	2
9	2	2
10	2	2
11	3	2
12	3	2
13	3	2
14	3	2

UCLA Statistical Consulting Group provides a workaround explained here.

# http://www.ats.ucla.edu/stat/spss/faq/kappa.htm

It requires using weighted data rather than unweight (ungrouped) data. Find the pattern of responses as explained earlier:

Essay	Essay Rater 1	Essay Rater 2	Pattern Rater 1	Pattern Rater 2	Frequency of Pattern
1	1	1	1	1	3
2	1	1	1	2	0
3	1	1	1	3	0
4	2	2	2	1	0
5	2	2	2	2	7
6	2	2	2	3	0
7	2	2	3	1	0
8	2	2	3	2	4
9	2	2	3	3	0
10	2	2			
11	3	2			
12	3	2			
13	3	2			
14	3	2			

For rater 2 there are no values of 3 used for rating essays; as the pattern of ratings above show, the frequency of rater 2 assigning a value of 3 is 0 (see highlighted cells).

To fool SPSS into calculating kappa, replace any one of the 0 frequencies highlighted above with a very small value, such as .0001. Use a small number so it does not influence calculation of kappa. See below:

Essay	Essay Rater 1	Essay Rater 2	Pattern Rater	Pattern Rater 2	Frequency of Pattern
1	1	1	1	1	3
2	1	1	1	2	0
3	1	1	1	3	0
4	2	2	2	1	0
5	2	2	2	2	7
6	2	2	2	3	0
7	2	2	3	1	0
8	2	2	3	2	4
9	2	2	3	3	.0001
10	2	2			
11	3	2			
12	3	2			
13	3	2			
14	3	2			

Now execute the crosstabs command again with these data (remember to assign Data-> Weight Case) and SPSS should provide the following kappa results.

b1p \* b2p Crosstabulation

		1.00	2.00	3.00	Total
b1p	1.00	3	0	0	3
	2.00	0	7	0	7
	3.00	0	4	0	4
Total		3	11	0	14

# Symmetric Measures

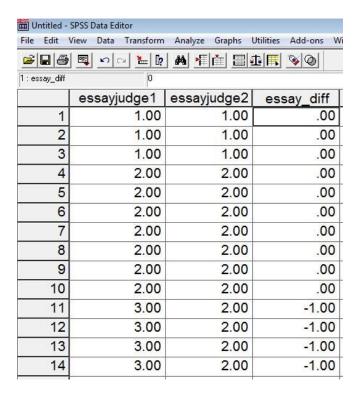
	Value	Asymp.Std. Error(a)	Approx. T(b)	Approx. Sig.
Measure of Agreement Kappa	.491	.177	3.159	.002
N of Valid Cases	14			

a Not assuming the null hypothesis.

b Using the asymptotic standard error assuming the null hypothesis.

Although you cannot see it, the frequency cell highlighted in gold above actually has the value .0001 but has been rounded to 0. Cohen's kappa is .491 for these data.

The percentage agreement for these data can be found as noted earlier by calculating the difference between judges then finding the percentage of agreements. The SPSS file with differences calculated follows:



The frequency display appears below.

		Frequency	Percent	Valid Percent	Cumulative Percent
Valid	-1.00	4	25.0	28.6	28.6
	.00	10	62.5	71.4	100.0
	Total	14	87.5	100.0	
Missing	System	2	12.5		
Total		16	100.0		

The percentage agreement is 71.4% (again, note that one should always use the "Valid Percent" column since it ignores missing data for calculating category percentages).

# 8. Krippendorff's Alpha: Two Raters

As noted kappa is not a universally accepted measure of agreement because calculation assumes independence of raters when determining level of chance agreement. As a result, kappa can be somewhat misleading. Viera and Garret (2005) provide an example of misleading kappa. Other sources discussing problems with kappa exist:

http://www.john-uebersax.com/stat/kappa.htm

http://en.wikipedia.org/wiki/Cohen's kappa

Krippendof's alpha (henceforth noted as K alpha) addresses some of the issues found with kappa, and is also more flexible. Details of the benefits of K alpha are discussed by Krippendorff (2011) and Hayes and Krippendorff (2007).

SPSS does not currently provide a command to calculate K alpha. Hayes and Krippendorff (2007) do provide syntax for running K alpha in SPSS. Copies of this syntax can be found at Hayes' website and I also have a copy on my site. The version on my site should be copied and pasted directly into SPSS syntax window.

http://www.afhayes.com/spss-sas-and-mplus-macros-and-code.html (see KALPHA)

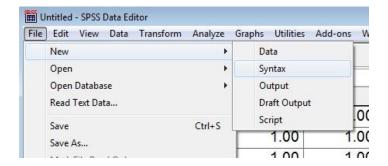
http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-krippendorff-alpha-SPSS.txt

#### 8a. K alpha with SPSS

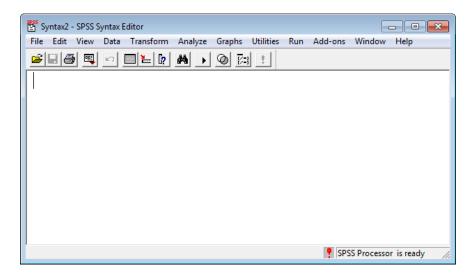
Note: To be updated – some with newer versions of SPSS had difficulty executing the Krippendorff alpha syntax; it may run or it may not. If you experience problems, use on-line websites to obtain alpha.

To copy and paste the K alpha commands into SPSS, do the following:

File  $\rightarrow$  New  $\rightarrow$  Syntax



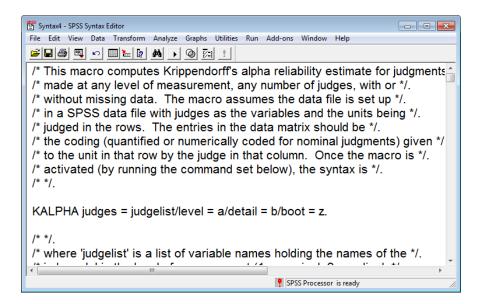
This opens a syntax window that should be similar to this window:



Now open the K alpha commands from this link

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-krippendorff-alpha-SPSS.txt

Next, copy and paste everything find at that link into the SPSS syntax window. When you finish, it should look like this:



To make this syntax work, four bits of the command line must be changed. The command line is the isolated line above that reads:

# KALPHA judges = judgelist/level = a/detail = b/boot = z.

# judges = judgelist

These are the raters which form columns in SPSS

#### level = a

This is the scale of measurement of ratings with

1 = nominal

2 = ordinal

3 = interval

4 = ratio

Since we are dealing with ratings that are nominal, select 1 here.

#### detail = b

Specify 0 or 1 here; by default select 1 to see calculations.

#### boot = z

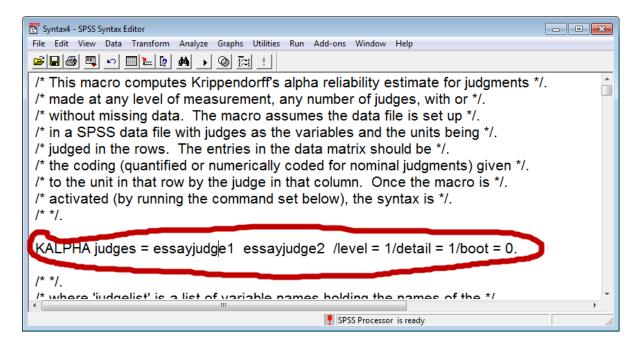
This option allows one to obtain bootstrapped standard errors for the K alpha estimate. For our purposes we won't request standard errors so place 0 for this option. If you wanted standard errors, the minimum replications would be 1000.

To obtain K alpha for the essay data below, make the following changes to the Kalpha command in the syntax window:

# KALPHA judges = essayreader1 essayreader2 /level = 1/detail = 1/boot = 0.

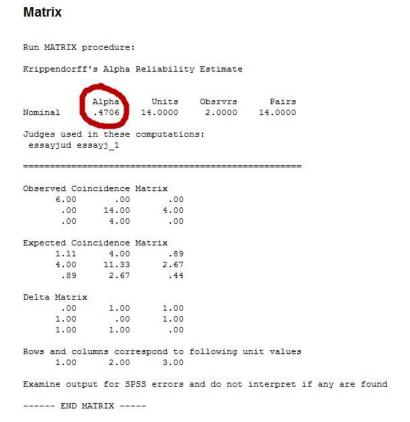
File Edit 1	/iew Data Transform	Analyze Graphs	Uti
	<u> </u>	M <u>*                                     </u>	1
10 : b_freq			
	essayjudge1	essayjudge2	
1	1.00	1.00	
2	1.00	1.00	
3	1.00	1.00	
4	2.00	2.00	
5	2.00	2.00	
6	2.00	2.00	
7	2.00	2.00	T
8	2.00	2.00	T
9	2.00	2.00	
10	2.00	2.00	T
11	3.00	2.00	
12	3.00	2.00	T
13	3.00	2.00	T
14	3.00	2.00	

The SPSS syntax window now looks like this:



To run this command, place the mouse cursor within the KALPHA command (anywhere in the command sentence), and then click on "Run Current" button which looks like this on my version of SPSS.

## **K Alpha SPSS output**



Krippendorff argues that values below .80 should be viewed as poor levels of agreement, so this value of .47 suggest problems with rater agreement.

## 8b K alpha with Online Calculators

Two web pages that provide indices of rater agreement are

http://dfreelon.org/utils/recalfront/

and

# https://nlp-ml.io/jg/software/ira/

Freelon's site provides four measures of agreement

- Percent agreement
- Scott's pi
- · Cohen's kappa
- Krippendorff's alpha

Geertzen's site provides four measures of agreement

- Percent agreement
- Fleiss's kappa (which is just Scott's pi for two judges)
- Krippendorff's alpha
- Cohen's kappa (if only 2 raters, mean kappa across more than 2 raters)

Note that Geertzen's site, <a href="https://nlp-ml.io/jg/software/ira/">https://nlp-ml.io/jg/software/ira/</a>, only addresses nominal rating categories. If one has ordinal, interval, or ratio ratings, then calculations from Geertzen's site may be inappropriate.

Scott's pi was designed for assessing agreement among two raters. Fleiss's kappa (Fleiss 1971) is an extension of Scott's pi to handle 2 or more raters. If only 2 raters are present, Fleiss's kappa = Scott's pi.

Freelon's site requires that the data be uploaded in CSV (comma-delimited format) with no headers of any sort. Each column represents a rater's scores, and each row is the object being rated. The essay data would look like this in a CSV file:

- 1,1
- 1,1
- 1,1
- 2,2
- 2,2
- 2,2
- 2,2
- 2,2
- 2,2
- 2,2
- 3,2
- 3,2
- 3,2
- 3,2

Geertzen's site requires similar data structure, but no commas and each column should have a header identifying the rater. There should be a blank space or tab between ratings and headers, like this:

rater1	rater2
1	1
1	1
1	1
2	2
2	2
2	2
2	2
2	2
2	2
2	2
3	2
3	2
3	2
3	2

For the essay data I have created two files suitable for use with Freelon's and Geertzen's sites.

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-Freelon-essay-data.csv

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-Geertzen-essay-data.txt

Download both files to your computer, then upload both to the respective websites.

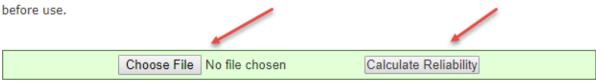
# Freelon's site (<a href="http://dfreelon.org/utils/recalfront/">http://dfreelon.org/utils/recalfront/</a>)

(a) Select the link for ReCal2 for nominal data and 2 coders.

Level of measurement	N of coders	Missing data allowed?	Use
Nominal	2 coders only	No /	ReCal2 (includes percent agreement, Scott's pi, Cohen's kappa, and nominal Krippendorff's alpha)
Nominal	2 or more coders	No	ReCal3 (includes pairwise percent agreement, Fleiss' kappa, pairwise Cohen's kappa, and nominal Krippendorff's alpha)
Nominal, ordinal, interval, or ratio	Any N of coders	Yes	ReCal OIR (includes nominal, ordinal, interval, and ratio Krippendorff's alpha with support for missing data)

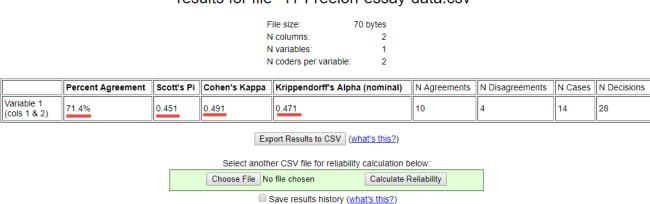
## (b) Chose the file to upload, the click "Calculate Reliability"

If you have used ReCal2 before, you may submit your data file for calculation via the form below. If you are a first-time user, please read the documentation first. (Note: failure to format data files properly may produce incorrect results!) You should also read ReCal's very short license agreement before use.



# (c) Note results

# ReCal 0.1 Alpha for 2 Coders results for file "11-Freelon-essay-data.csv"



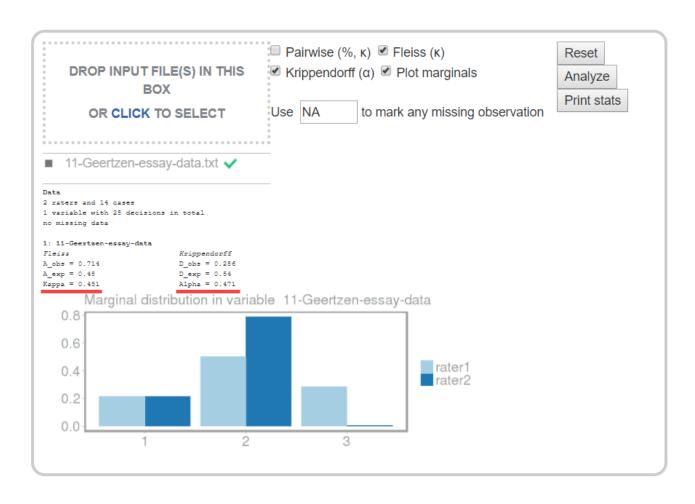
Percent agreement = 71.4 Scott's pi = .451 Cohen's kappa = .491 K alpha = .471

# Geertzen's site (https://nlp-ml.io/jg/software/ira/)

(a) Click "Reset" then drag the file to the drop box or "Click" to select files from your computer. Unfortunately, I was unable to obtain results with a check next to "Pairwise (%, κ)" so live that box blank otherwise an error will result.



- (b) Once uploaded, click select all options (except for the Pairwise box), then click "Analyze"
- (c) Note output



Fleiss kappa (Scott's pi) = .451

K alpha = .471

Percent agreement = not computed

Mean Conhen's kappa (if more than 2 raters, just kappa if only 2 raters) = not computed

# 9. Two-coder Examples

## 9a. Usefulness of Noon Lectures

What would be various agreement indices for Viera and Garret (2005) data in table 1?

#### Usefulness of Noon Lectures

		Resident 1— Lectures Helpful?				
		Yes	No	Total		
Resident 2—	Yes	15	5	20		
Lectures	No	10	70	80		
Helpful?	Total	25	75	100		

# 9b. Photographs of Faces

Example taken from Cohen, B. (2001). Explaining psychological statistics (2nd ed). Wiley and Sons.

There are 32 photographs of faces expressing emotion. Two raters asked to categorize each according to these themes: Anger, Fear, Disgust, and Contempt.

What would be the value of various fit indices these ratings?

**Ratings of Photographed Faces** 

		Rater 2				
	_	Anger	Fear	Disgust	Contempt	
	Anger	6	0	1	2	
Dator 1	Fear	0	4	2	0	
Rater 1	Disgust	2	1	5	1	
	Contempt	1	1	2	4	

Note: Numbers indicate counts, e.g., there are 6 cases in which raters 1 and 2 rated face as angry.

## 9c. Answers to 9a and 9b to be added.

# 10. Percent Agreement Among More than Two Raters

Recall the example of three raters provided above for hand calculation. The example is repeated below.

In situations with more than two raters, one method for calculating inter-rater agreement is to take the mean level of agreement across all pairs of reviewers.

Participant	Rater 1	Rater 2	Rater 3	Difference	Difference	Difference
				Pair 1 and 2	Pair 1 and 3	Pair 2 and 3
1	1	1	1	0	0	0
1	2	2	2	0	0	0
1	3	3	3	0	0	0
2	2	3	3	-1	-1	0
2	1	4	1	-3	0	3
3	2	3	1	-1	1	2
3	2	2	4	0	-2	-2
4	1	1	1	0	0	0
4	4	1	1	3	3	0
5	1	1	1	0	0	0
6	2	2	2	0	0	0
7	3	3	3	0	0	0
8	1	1	1	0	0	0
9	1	1	2	0	-1	-1
9	4	2	2	2	2	0
10	2	2	2	0	0	0
11	1	1	1	0	0	0
11	2	3	4	-1	-2	-1

Total count of 0 in difference column =	12	11	13
Total Ratings =	18	18	18
Proportion Agreement =	12/18 = .6667	11/18 = .6111	13/18 = .7222
Percentage Agreement =	66.67	61.11	72.22
Overall Percentage Agreement =	Mea	an agreement: 66.	67%

# 11. Mean Cohen's kappa for More than Two Raters

Some have suggested that one can calculate Cohen's kappa for each pair of raters, then take the mean value to form a generalized measure of kappa (Hallgren, 2012; Warrens, 2010). The limitations with kappa noted above still apply here. To illustrate, consider the data posted above for three raters.

For raters 1 and 2, kappa = .526 For raters 1 and 3, kappa = .435 For raters 2 and 3, kappa = .602

Mean kappa across all pairs = .521

## 12. Fleiss' kappa (pi) for More than Two Raters

As previously noted Fleiss extended Scott's pi to multiple raters, but Fleiss named it kappa as an extension of Cohen's kappa. The formula, however, follows more closely with Scott's version for calculating expected agreement than Cohen's version of expected agreement. This value can be interpreted like kappa. Illustrations will follow below.

# 13. Krippendorff's alpha for More than Two Raters

Krippendorff's alpha can be extended to any number of raters, and can also handle missing data well, something the above measures cannot handle well. Krippendorff's alpha is interpreted as noted before, with values below .80 viewed as weak agreement.

# 14. Three Rater Example: Percent Agreement, Cohen's Kappa Mean, Fleiss' kappa, Krippendorff's alpha

The three-rater data, presented above in "9. Percent Agreement Among More than Two Raters," will be used finding agreement measures using Freelon's and Geertzen's websites, and also SPSS with Krippendorff's alpha command syntax.

## 14a. Freelon's site <a href="http://dfreelon.org/utils/recalfront/">http://dfreelon.org/utils/recalfront/</a>

The data file for Freelon's site should follow the format shown below.

1, 1, 1 2, 2 2, 3, 3, 3 3 2, 3, 1, 4, 1 2, 3, 1 2, 2, 4 1, 1, 1 4, 1, 1 1, 1 1, 2 2, 2, 3 3, 3, 1, 1, 1 1, 2 1,

2,

2,

1, 3,

4,

2,

1,

2,

These data are located in the following file.

2

2

4

http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-Freelon-three-raters.csv

# On Freelon's site select option for 3+ raters:

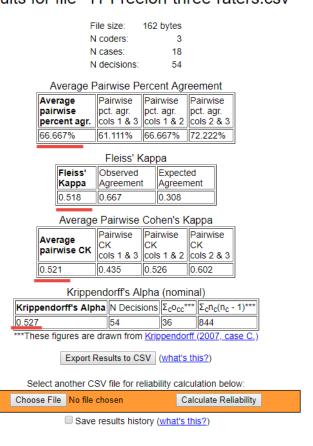
Level of measurement	N of coders	Missing data allowed?	Use
Nominal	2 coders only	No	ReCal2 (includes percent agreement, Scott's pi, Cohen's kappa, and nominal Krippendorff's alpha)
Nominal	2 or more coders	No	ReCal3 (includes pairwise percent agreement, Fleiss' kappa, pairwise Cohen's kappa, and nominal Krippendorff's alpha)
Nominal, ordinal, interval, or ratio	Any N of coders	Yes	ReCal OIR (includes nominal, ordinal, interval, and ratio Krippendorff's alpha with support for missing data)

Then on the new page upload the data file and click "Calculate Reliability" as shown below.



#### Results are reported below

# ReCal 0.1 Alpha for 3+ Coders results for file "11-Freelon-three-raters.csv"



Percentage agreement = 66.7 Mean Cohen's kappa (pairwise kappa) = .521 Fleiss' kappa = .518 Krippendorff's alpha = .527

All suggest low agreement among raters.

# 14b. Geertzen's site <a href="https://nlp-ml.io/jg/software/ira/">https://nlp-ml.io/jg/software/ira/</a>

The data file for Geertzen's site should follow the format shown below.

R1	R2	R3
1	1	1
2	2	2
3	3	3
2	3	3
1	4	1
2	3	1
2	2	4
1	1	1
1 4	1	1
1	1	1
2	2	2
3	3	3
1	1	1
1	1	2
4	2	2
2	2	2
1	1	1
2	3	4

Here is a text file with these data:

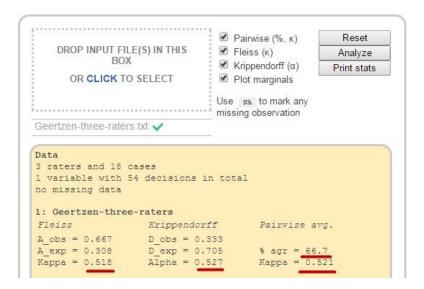
http://www.bwgriffin.com/gsu/courses/edur9131/2018spr-content/11-coder-agreement/11-Geertzen-three-raters.txt

Follow the steps outlined earlier – (a) Click Reset if any results are current presented, (b) upload or drag the data file to the input box, and (c) select those statistics of interest.

As noted before, I was unsuccessful obtain Cohen's kappa and Pairwise percentages, so remove the check mare from the Pairwise box and the page is then able to estimate Fleiss's kappa and Krippendorff's alpha.



Below is output from an earlier version of the page with functioning Pairwise percentages and Cohen's kappa.



Percentage agreement = 66.7 (same as reported in hand calculation)

Mean Cohen's kappa (pairwise kappa) = .521 (same as found with mean kappa in SPSS)

Fleiss kappa = .518

Krippendorff alpha = .527

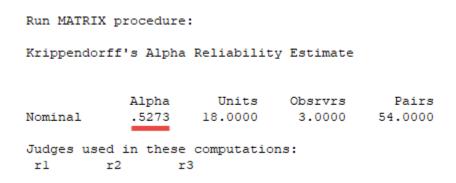
# **14c. SPSS**The three-rater data noted above are entered into SPSS as follows:

888	r .	21	
	r1	r2	r3
1	1.00	1.00	1.00
2	2.00	2.00	2.00
3	3.00	3.00	3.00
4	2.00	3.00	3.00
5	1.00	4.00	1.00
6	2.00	3.00	1.00
7	2.00	2.00	4.00
8	1.00	1.00	1.00
9	4.00	1.00	1.00
10	1.00	1.00	1.00
11	2.00	2.00	2.00
12	3.00	3.00	3.00
13	1.00	1.00	1.00
14	1.00	1.00	2.00
15	4.00	2.00	2.00
16	2.00	2.00	2.00
17	1.00	1.00	1.00
18	2.00	3.00	4.00

Using Haye's K alpha syntax, the following command line is used:

# KALPHA judges = r1 r2 r3 /level = 1/detail = 1/boot = 0.

The three judges are raters 1, 2, and 3, denoted in SPSS as r1, r2, and r3. Level = 1 which means these are nominal scaled ratings (categorical), and detail is 1 means calculations should be reported. Book = 0 means no bootstrapping is to occur.



## 15. Missing Data

Suppose four raters were asked to code 14 passages of text with the following codes. The table below shows results of their coding.

#### **Coding Options:**

- 1 = Positive statement
- 2 = Negative statement
- 3 = Neutral statement
- 4 = Other unrelated statement/Not applicable

Passage	Rater 1	Rater 2	Rater 3	Rater 4
1	1	2	1	
2	1	2		
3		1	1	1
4	1			
5	1	1	2	1
6	2		2	
7		1		1
8	2		3	
9		2	2	
10	3			3
11	3			2
12			1	1
13	4			4
14	4	4	-	

Note that several cells are empty; this means a code was not supplied by a rater. For example, for Passage 1, Rater 4 did not provide a code. With some passages 2 raters provided codes, 3 raters provided codes, or 4 raters provided codes. Notice also that passage 4 has only one rater, so information from that passage cannot be used to calculate level of agreement since all methods for calculating method of agreement requires at least two raters.

This creates problems for Fleiss's kappa and even makes it difficult to determine how best to calculate percent agreement because some passages will have more raters than others so this creates a problem of weighting percentages.

Krippendorff's alpha, however, is designed to address such missing data and still provide a measure of rater agreement.

Instructor note: To see difficulties calculating simple percentage agreement with multiple raters and missing data, see three different percent agreement results in this Excel file content/MultipleRatersAgreementPercent.xlsx, three estimates are 72.43%, 65.27%,67.94%, and 63.63%, none of which agree with Geertzen's value of 58.3%)

# 15a. Freelon's site <a href="http://dfreelon.org/utils/recalfront/">http://dfreelon.org/utils/recalfront/</a>

To obtain Krippendorff's alpha with Freelon's site, replace all missing values with #, then upload the data file as illustrated earlier.

1	2	1	#
1	2	#	#
#	1	1	1
1	#	#	#
1	1	2	1
2	#	2	#
#	1	#	1
2	#	3	#
#	2	2	#
3	#	#	3
3	#	#	2
#	#	1	1
4	#	#	4
4	4	#	#

Results from Freelon's site; K alpha = .531.

# ReCal for Ordinal, Interval, and Ratio-Level Data results for file "11-Freelon-four-missing.csv"

File size: 134 bytes N coders: 4 N cases: 13 N decisions: 30



Select another CSV file for reliability calculation below:



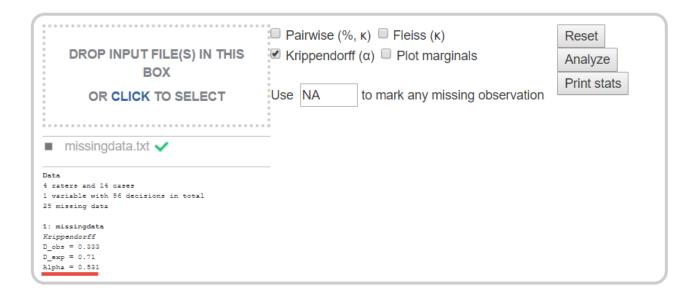
■ Save results history (what's this?)

# 15b. Geertzen's site <a href="https://nlp-ml.io/jg/software/ira/">https://nlp-ml.io/jg/software/ira/</a>

Geertzen's site can be used to find Krippendorff's alpha. To identify missing data, Geertzen requires that missing data be denoted with NA (capital NA, "na" won't work). Below is a revised table to meet Geertzen's specifications.

Rater 1	Rater 2	Rater 3	Rater 4
1	2	1	NA
1	2	NA	NA
NA	1	1	1
1	NA	NA	NA
1	1	2	1
2	NA	2	NA
NA	1	NA	1
2	NA	3	NA
NA	2	2	NA
3	NA	NA	3
3	NA	NA	2
NA	NA	1	1
4	NA	NA	4
4	4	NA	NA

Results of Geertzen's calculations are presented below. K alpha = .531. The page won't calculate alpha if other statisitics are requested (e.g., Pariwise or Fleiss).

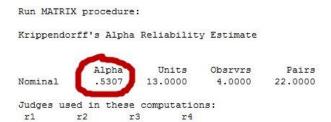


## 15c. SPSS

The SPSS syntax by Hayes also produces the same value of K alpha. See below. Leave missing data as blank in the SPSS data sheet – see example below.

13.11	J				
	r1	r2	r3	r4	\
1	1.00	2.00	1.00		
2	1.00	2.00			
3		1.00	1.00	1.00	
4	1.00				
5	1.00	1.00	2.00	1.00	
6	2.00		2.00		
7		1.00		1.00	
8	2.00		3.00		
9		2.00	2.00		
10	3.00			3.00	
11	3.00			2.00	
12			1.00	1.00	
13	4.00			4.00	
14	4.00	4.00			
15					
1.0					

Output from Hayes' k-alpha syntax appears below.



Supplemental: For those with Stata, here's the command and output to obtain K-alpha with Stata.

. kalpha var1 var2 var3 var4, scale(n) transpose bootstrap(reps(5000) minalpha(.8) dots(10))

Krippendorff's Alpha-Reliability (nominal data)

No. of units = 13 No. of observers = 4 Krippendorff's alpha = 0.531

**Bootstrap** results

No. of coincidences = 30 Replications = 5000

> [95% Conf. Interval] 0.343 0.718

Probability of failure to reach alpha

min. alpha q 0.800 0.999

Assumes columns are cases and rows coders, so use transpose if columns are coders and rows are cases.

# 16. High Agreement Yet Low Kappa and Alpha

Measures of rater agreement often provide low values when high levels of agreement exist among raters. The table below shows 20 passages coded by four raters using the four coding categories listed below. Note that all raters agree on every passage except for passage 20.

Despite 95.2% agreement, the other measures of agreement are below acceptable levels: Fleiss' kappa = .316, mean Cohen's kappa = .244, and Krippendorff's alpha = .325.

1 = Positive statement

2 = Negative statement

3 = Neutral statement

4 = Other unrelated statement/Not applicable

The problem with these data is lack of variability in codes. When most raters assign one code predominately, then measures of agreement can be misleadingly low, as demonstrated in this example. This is one reason I recommend always reporting percent agreement.

Passage	Rater1	Rater2	Rater3	Rater4
1	1	1	1	1
2	1	1	1	1
3	1	1	1	1
4	1	1	1	1
5	1	1	1	1
6	1	1	1	1
7	1	1	1	1
8	1	1	1	1
9	1	1	1	1
10	1	1	1	1
11	1	1	1	1
12	1	1	1	1
13	1	1	1	1
14	1	1	1	1
15	1	1	1	1
16	1	1	1	1
17	1	1	1	1
18	1	1	1	1
19	1	1	1	1
20	4	3	2	1

Results from Freelon's site.

# Average Pairwise Percent Agreement

Average	Pairwise	Pairwise	Pairwise	Pairwise	Pairwise	Pairwise
pairwise percent agr.		pct. agr. cols 1 & 3				pct. agr. cols 3 & 4
						95%

# Fleiss' Kappa

Fleiss'	Observed	Expected
Kappa	Agreement	Agreement
0.316	0.95	0.927

# Average Pairwise Cohen's Kappa

Average pairwise CK	CIZ	CIZ	CIZ	CIZ	CIZ	Pairwise CK cols 3 & 4
0.244			0.487		0.487	-0

# Krippendorff's Alpha (nominal)

Krippendorff's Alpha	N Decisions	$\Sigma_{C}o_{CC}^{***}$	$\Sigma_{c}$ n <sub>c</sub> (n <sub>c</sub> - 1)***
0.325	80	76	5852

<sup>\*\*\*</sup>These figures are drawn from Krippendorff (2007, case C.)

## 17. Patterns of Response, Bias in Coding Categories, Kappa Paradoxes

This section is under development and not yet ready for use.

Joyce (2013) presents the following tables

http://digital-activism.org/2013/05/picking-the-best-intercoder-reliability-statistic-for-your-digital-activismcontent-analysis/

Figure 5: The Weakness of Cohen's Kappa

							Coder A			
Categories	•	a	b	c			a	b	c	
Curegories	a	12	9	9	30	a	12	18	18	48
Coder B	ь	9	14	9	32	b	0	14	18	32
	c	9	9	20	38	c	0	0	20	20
		30	32	38	100		12	32	56	100
		$\mathbf{A}_{0}$	=	.460			$\mathbf{A}_{0}$	=	.460	
		π	=	.186			π	=	.186	
		K	=	.186			K	=	.258	

Percent agreement = 46.0%	Percent agreement = 46.0%				
Scott's pi = .186	Scott's pi = .186				
Cohen kappa = .186	Cohen kappa = .258				
K alpha for first table = .1836	K alpha for first table = .1898				

Note how kappa is influenced by the pattern of response whereas neither pi nor alpha are affected or greatly affected.

Stata output for K alpha (same results for both tables):

. kalpha var1 var2, scale(n) transpose

Krippendorff's Alpha-Reliability (nominal data)

No. of units = 100 No. of observers = 2 Krippendorff's alpha = 0.190

Example tables of paradoxes for kappa: <a href="http://folk.ntnu.no/slyderse/Pres24Jan2014.pdf">http://folk.ntnu.no/slyderse/Pres24Jan2014.pdf</a> (in folder as 2014 Lydersen Paradoxes with Agreement Measures.pdf )

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